



Investigating Potential Strategy Flexibility in Linear Algebra

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Introduction

- The frequent problem within the education system is recalling ways to solve a problem using the most effective method.
- Participants have trouble using the most effective solution
- Knowledge of strategies are related to strategy selection (Xu et al., 2017; Liu et al., 2018)
- Current study investigates potential strategy flexibility.
- potential strategy flexibility:
 - knowledge of the strategy
 - knowledge of multiple strategies
 - knowledge of strategy efficiency
- We predict that participants with more knowledge of multiple strategies will have high knowledge of strategy validity and strategy efficiency.

Abstract

Previous studies have found that students know multiple strategies to solve a given problem but do not always use the best strategy to solve it (Liu et al., 2018; Hickendorff, 2020). The current study is interested in investigating potential strategy flexibility. We define potential strategy flexibility as consisting of knowledge of strategy validity, knowledge of multiple strategies, and knowledge of strategy efficiency. We predict that students with more knowledge of multiple strategies will have high knowledge of strategy validity and strategy efficiency. In the current study, college students were given three different tasks in algebra. To assess their knowledge of multiple strategies, participants were given 12 linear equation problems and asked to generate as many solutions as possible. To assess their knowledge of strategy validity, participants received 36 solved linear equation problems. The solutions reflected standard strategies, innovative strategies, and wrongly executed strategies and participants were asked to judge the validity of each solution. We tested their knowledge of strategy efficiency by showing them two different solutions for the same problem, reflecting the standard and innovative strategy, and asking them to choose the strategy they think is better. The current study is still ongoing, result will be available by the time of the symposium.

Methods

Participants

- 11 undergraduate students from a large public university located in the south of U.S
- 2 participants completed the knowledge strategy validity task and the knowledge of strategy efficiency task.

Measure

Problem	Standard algorithm	Innovative strategy
$4(x - 2) = 24$	Begin by distributing the parentheses	$4x - 4 \times 2 = 24$ Divide a constant to both sides before distributing
$5(x + \frac{3}{2}) + 3(x + \frac{3}{2}) = 16$	Begin by distributing the parentheses	$x - 2 = 24/4$
$5(x + 0.6) + 3x = 5(x + 0.6) + 7$	Begin by distributing the parentheses	Change in variable-combine
$\frac{2x - 6}{2} - \frac{6x - 18}{3} = 5$	Begin by obtaining a common denominator for the two algebraic expressions	Change in variable-subtract from both
		$8(x + \frac{3}{2}) = 16$
		$3x = 7$
		$(x - 3) + (2x - 6) = 5$
		Reducing each fraction before combining

Knowledge of multiple strategies

Participants were asked to generate as much different strategies to a given algebra problem

Knowledge of Strategy Validity

Participants were asked to judge the validity of a given solution (standard, innovative, wrong)

Knowledge of Strategy Efficiency

Participants compared two solutions (standard vs. Innovative)

1. $8(x - \frac{1}{2}) - 3 = 6(x - \frac{1}{2})$

Please show your work here:

Please write your answer here:

2. $16 = 5(x - 2) + 4(x - 2) - (x - 2)$

Show your work here:

Write your answer here:

Is the above solution correct? Please circle your answer: Yes No

Please look at both solutions and circle the solution you think will take less steps.

1. $\frac{(2x + 3)}{3} + \frac{(4x + 4)}{4} = 4$

Show your work here:

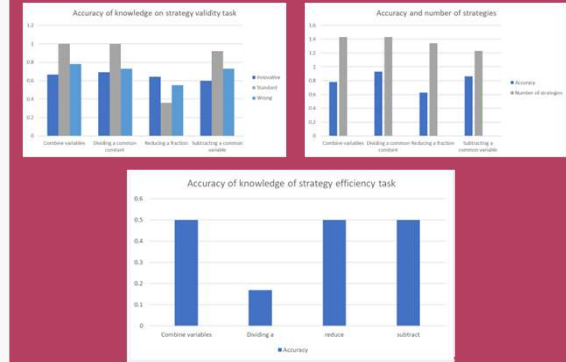
Write your answer here:

2. $\frac{(2x + 3)}{3} + \frac{(4x + 4)}{4} = 4$

Show your work here:

Write your answer here:

Results



Discussion

- On average participants have low knowledge to give multiple strategies to solve the problems
- They do not always view innovative strategies are valid
- They do not view innovative strategies as more efficient
- Our results are different from past studies because our participants have lower knowledge of multiple strategies
- Demonstrating innovative strategies in school can help students create multiple ways to solve problems

References

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Xu et al. (2017). Measures of potential flexibility and practical flexibility in equation solving. *Frontiers in psychology*